



University
of Glasgow

Enhancing cross-
disciplinary mathematical skills
through a collaborative
e-assessment initiative

LTC Presentation 2022

NUMBAS

Numbas at Glasgow

- Previous projects (Chemistry, Life Sciences)
- Other existing use (Geospatial, Access)
- Further potential (Maths Support, more questions, other subject areas)
- Project team and Chancellor's Fund
- Recruitment of undergraduate student project assistants
 - Named appointments
 - 3 x 80 hours (~5 hours a week for 4 months)
 - Support from Newcastle

Project Team



Elizabeth Petrie, GES



Michael O'Connor
2nd year Economics



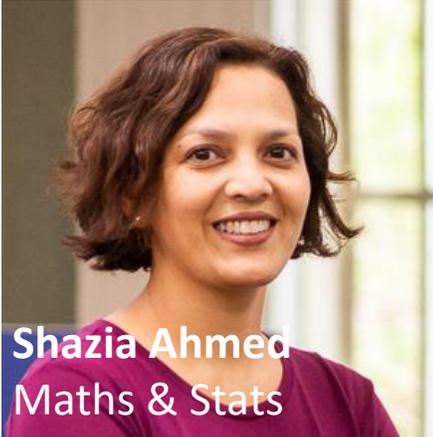
Beth Paschke
Chemistry



Clare Brown,
Lifelong learning



Ruth Douglas
Maths Adviser (SLD)



Shazia Ahmed
Maths & Stats



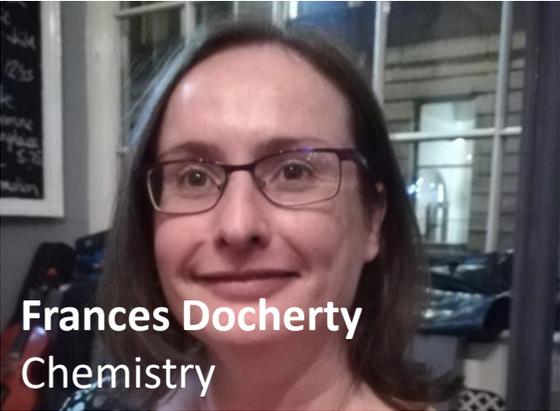
Anna Cartlidge
2nd year Economics



William Finlay
Finance (ASBS)



Niall Barr, CoSE



Frances Docherty
Chemistry



Tess Lynn
3rd year Chemistry

Project team development interests

- **Frances Docherty & Beth Paschke**, Chemistry: Maths support for chemists, online lab reporting, practice exercises on lecture material, maths support for science fundamentals course
- **Clare Brown**, Lifelong Learning: self-diagnostic assessment for prospective students, practice questions for mastering key skills
- **Ruth Douglas**, Maths Support resources for students requiring extra practice on particular topics; Access Maths formative tests and practice exercises
- **William Finlay**, Adam Smith Business School: Building maths confidence without the need for as much staff involvement, creating an accessible learning environment
- **Elizabeth Petrie**, GES: Geospatial PGT - improve by increased variety in Q pool

Numbas

- Online assessment system designed for mathematical subjects
- Free to use and open source
- Designed for accessibility
- Adaptive marking & diagnostic and explore modes
- Graphics and programming
- Lots of info at:
<https://www.numbas.org.uk>

Simplify the following expression by combining "like" terms.

$$7x - 3 - 3x^2 + 8x + 5$$

✓

✓ Your answer is numerically correct. You were awarded 1 mark.
You scored 1 mark for this part.

Score: 1/1 ✓
Answered

Submit answer

Score: 1/1 ✓

Try another question like this one

Reveal answers

- If questions are ready, creating an exam is simple:
- Put questions in 'shopping basket' and decide on exam settings
 - Import the exam package to Moodle and set up

Possibilities

Consider strategy/needs carefully, test, evaluate including student feedback

Use	Randomisation
Additional optional student resource	Students can keep practicing areas they find difficult
Formative testing	Allows repeated tests
Low credit summative testing	Allows repeated tests and keep max score.
Summative testing – can be review tests	Numerical answers can be different for each student
Diagnostic testing	Numerical answers can be different for each student

Example - GES PGT mixed experience maths

- Numbas approach evolved and tested over three years
- Assessment 10% of 20 credit module
- 10 weekly tests (minimal credit, repeat as wish before deadline)
- 2 review tests (single timed sitting, most of credit)
- Further experience with Lab reporting in Chemistry



Glasgow Numbas Question Pool

+ New: Folder Question Exam

8 items in this folder.

Select all Select none

Status	Name	Type	Last modified
<input type="checkbox"/>	Basic Algebra Skills		
<input type="checkbox"/>	Basic Statistics		
<input type="checkbox"/>	Basic Trigonometry and Pythagoras		
<input type="checkbox"/>	Linear Graphs		
<input type="checkbox"/>	Logs and Exponentials		
<input type="checkbox"/>	Numeracy		
<input type="checkbox"/>	Quadratics		
<input type="checkbox"/>	Roots and Indices		

Undergraduate Project Assistants



Anna Cartlidge



Tess Lynn



Michael O'Connor

65 results for "logs".

Show results for

- Questions
- Exams

Refine by

- Status
 - Any status
 - Draft
 - Ready to use
 - Should not be used
 - Has some problems
 - Doesn't work
 - Needs to be tested

Author

Equations involving logs



Ready to use

Exam (5 questions) in Martin's workspace by Martin Jones

Solve equations involving logs and exponential functions, by using inverse operations.

Equations involving logs



Ready to use

Exam (5 questions) in Glasgow Numbas Question Pool by Tess Lynn and 1 other

Solve equations involving logs and exponential functions, by using inverse operations.

Solving exponential equations using logs



Ready to use

Question in Glasgow Numbas Question Pool by Tess Lynn and 1 other

No description given

Combining use of multiple laws of logarithms into one equation



Ready to use

Question in Glasgow Numbas Question Pool by Tess Lynn and 3 others

Given a sum of logs, all numbers are integers,

$\log_b(a_1) + \alpha \log_b(a_2) + \beta \log_b(a_3)$ write as $\log_b(a)$ for some fraction a .

Also calculate to 3 decimal places $\log_b(a)$.

Advice

Edit ▾ Insert ▾ View ▾ Format ▾ Table ▾ Tools

↶ ↷ Formats ▾ ☰ ☷ **B** *I* U ☰

In order to solve this question, you need to identify

Therefore to solve for the future value:

We know that the PV is £{num_PV}million, we know that r = {num_return*100}% and we have {num_period} periods of compounding. Therefore:

Advice

In order to solve this question, you need to identify that we are solving for this equation:

$$FV = PV(1 + r)^n$$

Therefore to solve for the future value:

$$FV = PV(1 + r)^n$$

We know that the PV is £{num_PV}million, we know that $r = \{num_return \cdot 100\}\%$ and we have {num_period} periods of compounding. Therefore:

$$FV = PV(1 + r)^n$$

$$FV = \{num_{PV}\} (1 + \{num_return\})^{\{num_period\}}$$

$$FV = \{answer\} \text{ million}$$

A government bond issued in {place} has a coupon rate of {coupon}%, face value of €{face} and the bond matures in {period_years} years.

Assuming that the coupons are paid on an annual basis. Calculate the price of a bond (in euro) if the yield to maturity is {ytm}%.

€

[Click to edit](#)

Alternative approach

You may also solve

The future value should be rounded to 4 decimal places.

[Click to edit](#)

€ Round your answer to 2 decimal places.

✓ You were awarded 1 mark.
You scored 1 mark for this part.

Score: 1/1 ✓
Answered

Submit answer

Example Question

Answer the question below:

PV_bond

A government bond issued in France has a coupon rate of 2.1%, face value of €100 and the bond matures in 30 years.

Assuming that the coupons are paid on an annual basis. Calculate the price of a bond (in euro) if the yield to maturity is 4%.

€ Round your answer to 2 decimal places.

Submit answer

Score: 0/1

Try another question like this one

Reveal answers

Questions?

If interested:

- info and demo of question types at: <https://www.numbas.org.uk/>
- contact one of the project team:

Ruth Douglas	Ruth.Douglas@glasgow.ac.uk
Elizabeth Petrie	Elizabeth.Petrie@glasgow.ac.uk
Niall Barr	Niall.Barr@glasgow.ac.uk
William Finlay	William.Finlay@glasgow.ac.uk
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Beth Paschke	Beth.Paschke@glasgow.ac.uk
Frances Docherty	Frances.Docherty@glasgow.ac.uk
Clare Brown	Clare.Brown.2@glasgow.ac.uk

**Thanks
for
listening!**

Appendix - Examples

Examples

Writing the question in NUMBAS:

Write the question

A government bond issued in {place} has a coupon rate of {coupon}%, face value of €{face} and the bond matures in {period_years} years.

Assuming that the coupons are paid on an annual basis. Calculate the price of a bond (in euro) if the yield to maturity is {ytm}%.

€

[Click to edit](#)

Define the variables

Name

Data type
Random number from a range

Value
A random number between and (inclusive) with step size

Description

[Click to edit](#)

Describe what this variable represents, and list any assumptions made about its value.

Can an exam override the value of this variable?

→ Used by:

📄 Ungrouped variables				
	Name	Type	Generated Value	
🔒	↔ coupon	number	8.6	✖
🔒	↔ period_years	integer	45	✖
🔒	↔ ytm	number	1.6	✖
🔒	coupon_dec	number	0.086	✖
🔒	ytm_dec	number	0.016	✖
🔒	PVAF_dec	number	31.9041051506	✖
🔒	face	integer	100	✖
🔒	coupon_payme nt	number	8.6	✖
🔒	PVIF_dec	number	0.4895343176	✖
🔒	PV_bond	number	323.33	✖
🔒	↔ place	string	the Netherlands	✖

Examples

Writing the question in NUMBAS:

Write advice

Advice

In order to solve this question, we need to recognize that we are trying to solve the present value of a government bond.

To calculate the price of a bond:

$$PV_{bond} = coupon * \left(\frac{1}{r} - \frac{1}{r(1+r)^n} \right) + \frac{Par}{(1+r)^n}$$

Using the information provided in the question:

The coupon is {currency({coupon_payment},"€","p")}, this is calculated as {coupon}% of the face value of €{face}. The number of periods in this problem is {period_years} and the yield to maturity is {ytm}%.

Therefore to solve the value of this bond from {place}:

$$PV_{bond} = \{coupon_payment\} * \left(\frac{1}{\{ytm_dec\}} - \frac{1}{\{ytm_dec\}(1+\{ytm_dec\})^{\{period_years\}}} \right) + \frac{\{face\}}{1+\{ytm_dec\}^{\{period_years\}}}$$

The present value of the bond = {currency(PV_bond,"€","cents")}

[Click to edit](#)

Examples

Student facing NUMBAS:

The question

Answer the question below:

PV_bond

A government bond issued in France has a coupon rate of 2.1%, face value of €100 and the bond matures in 30 years.

Assuming that the coupons are paid on an annual basis. Calculate the price of a bond (in euro) if the yield to maturity is 4%.

€ Round your answer to 2 decimal places.

€ Round your answer to 2 decimal places.

Submit answer

Score: 0/1

Try another question like this one

Reveal answers

✔ You were awarded 1 mark.

You scored 1 mark for this part.

Score: 1/1 ✔

Answered

Submit answer

Score: 1/1 ✔

Examples

Student facing NUMBAS:

Advice

Advice

In order to solve this question, we need to recognize that we are trying to solve the present value of a government bond.

To calculate the price of a bond:

$$PV_{bond} = coupon * \left(\frac{1}{r} - \frac{1}{r(1+r)^n} \right) + \frac{Par}{(1+r)^n}$$

Using the information provided in the question:

The coupon is €2.10, this is calculated as 2.1% of the face value of €100. The number of periods in this problem is 30 and the yield to maturity is 4%.

Therefore to solve the value of this bond from France:

$$PV_{bond} = 2.1 * \left(\frac{1}{0.04} - \frac{1}{0.04(1+0.04)^{30}} \right) + \frac{100}{1+0.04^{30}}$$

The present value of the bond = €67.15

Examples

Student facing NUMBAS:

Infinite number of questions

PV_bond

A government bond issued in Germany has a coupon rate of 1.8%, face value of €100 and the bond matures in 27 years.

Assuming that the coupons are paid on an annual basis. Calculate the price of a bond (in euro) if the yield to maturity is 5.9%.

PV_bond

A government bond issued in France has a coupon rate of 3.4%, face value of €100 and the bond matures in 2 years.

Assuming that the coupons are paid on an annual basis. Calculate the price of a bond (in euro) if the yield to maturity is 13.6%.

PV_bond

A government bond issued in Italy has a coupon rate of 9%, face value of €100 and the bond matures in 30 years.

Assuming that the coupons are paid on an annual basis. Calculate the price of a bond (in euro) if the yield to maturity is 10.2%.

PV_bond

A government bond issued in the Netherlands has a coupon rate of 6.3%, face value of €100 and the bond matures in 36 years.

Assuming that the coupons are paid on an annual basis. Calculate the price of a bond (in euro) if the yield to maturity is 15.6%.

PV_bond

A government bond issued in Italy has a coupon rate of 3.6%, face value of €100 and the bond matures in 5 years.

Assuming that the coupons are paid on an annual basis. Calculate the price of a bond (in euro) if the yield to maturity is 16.8%.

PV_bond

A government bond issued in the Netherlands has a coupon rate of 4.6%, face value of €100 and the bond matures in 8 years.

Assuming that the coupons are paid on an annual basis. Calculate the price of a bond (in euro) if the yield to maturity is 3.4%.

PV_bond

A government bond issued in Italy has a coupon rate of 9.5%, face value of €100 and the bond matures in 26 years.

Assuming that the coupons are paid on an annual basis. Calculate the price of a bond (in euro) if the yield to maturity is 19.3%.

